

# EXPERIMENTAL ANALYSIS OF CHIP FORMATION AND CHIP BREAKING PROCESS IN METAL CUTTING

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In partial fulfillment of the requirements for the award of the degree  
of  
Bachelor of Science in Mechanical Engineering

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## **Abstract**

This thesis investigates the phenomenon of chip formation and chip breaking process in metal cutting, which is a crucial aspect of modern manufacturing processes. The objective of this study is to understand the mechanisms involved in the formation and breaking of chips, and to analyze and understand chip formation and the breaking process thoroughly, enabling accurate predictions.

The analysis was conducted by extensively investigating various cutting parameters, such as cutting speed, feed rate, and depth of cut. The experimental study encompassed a wide range of metallic materials, including aluminum, brass, and stainless steel.

The results of the study demonstrate that the chip formation and breaking process in metal cutting is a complex phenomenon that is affected by various factors such as material properties, cutting parameters, and tool geometry. Through detailed analysis, accurate predictions of chip formation and the breaking process were achieved. These predictions serve as a valuable tool for optimizing cutting parameters and enhancing overall machining performance.

The findings of this study have significant implications for the manufacturing industry, where the optimization of machining parameters can lead to significant improvements in productivity, quality, and cost-effectiveness. The analysis provides valuable insights for the industry to achieve these goals and enhance their competitiveness in the global market.

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## Notation

| Symbol     | Description                                | Units         | Symbol     |
|------------|--|---------------|------------|
| $V_c$      | Cutting speed                              | m/min         | $V_c$      |
| $f$        | Feed rate                                  | mm/tooth      | $f$        |
| $d$        | Depth of cut                               | mm            | $d$        |
| $t$        | Tool life                                  | min           | $t$        |
| $f_n$      | Chip thickness in the primary shear zone   | mm            | $f_n$      |
| $f_v$      | Chip thickness in the secondary shear zone | mm            | $f_v$      |
| $\alpha$   | Shear angle                                | degrees       | $\alpha$   |
| $P$        | Cutting force                              | N             | $P$        |
| $P_m$      | Maximum cutting force                      | N             | $P_m$      |
| $T_{max}$  | Maximum temperature                        | °C            | $T_{max}$  |
| $R_z$      | Surface roughness                          | $\mu\text{m}$ | $R_z$      |
| $T_c$      | Tool-chip contact length                   | mm            | $T_c$      |
| CEC        | Chip compression ratio                     | -             | CEC        |
| ODT        | Orthogonal cutting distance                | mm            | ODT        |
| $E$        | Modulus of elasticity                      | GPa           | $E$        |
| $\nu$      | Poisson's ratio                            | -             | $\nu$      |
| $\epsilon$ | Strain                                     | -             | $\epsilon$ |
| $\tau$     | Shear stress                               | MPa           | $\tau$     |
| $\eta$     | Efficiency                                 | %             | $\eta$     |
| $N$        | Number of teeth                            | -             | $N$        |
| $V_f$      | Feed speed                                 | mm/min        | $V_f$      |
| Rake       | Rake angle                                 | degrees       | Rake       |
| $\alpha_c$ | Clearance angle                            | degrees       | $\alpha_c$ |
| $R_a$      | Arithmetic average roughness               | $\mu\text{m}$ | $R_a$      |
| $R_t$      | Total roughness                            | $\mu\text{m}$ | $R_t$      |
| $R_q$      | Root-mean-square roughness                 | $\mu\text{m}$ | $R_q$      |
| $R_{sk}$   | Skewness                                   | -             | $R_{sk}$   |
| $R_{ku}$   | Kurtosis                                   | -             | $R_{ku}$   |

In this example, the notation appendix provides a list of symbols commonly used in the study of chip formation and breaking, along with a brief description of each symbol and the units used for each variable. The notation helps to standardize the language used in the thesis and allows readers to easily understand the meaning of each symbol.

This list includes all the symbols and abbreviations used in the thesis, along with a brief description of each symbol and the units used for each variable. It is important to note that this is just an example and that the actual notation used in the thesis may differ depending on the specific study and field of research.



## **Chapter 1**

### **Introduction**

The introduction begins by highlighting the importance of metal cutting in modern manufacturing industries and the need to optimize the machining process to reduce costs, increase efficiency, and improve the quality of the machined parts. The chapter then reviews the history of metal cutting and the evolution of theories and understanding related to chip formation and chip breaking, highlighting the gaps and limitations in the existing knowledge.

The chapter then outlines the specific objectives of the study, which are to investigate the chip formation and chip breaking process in metal cutting, to analyze and predict chip morphology, cutting forces, and tool wear, and to validate these findings experimentally. Finally, the chapter provides an overview of the methodology and approach adopted in the study, including the experimental setup, data collection and analysis, and the statistical and regression analysis techniques used to analyze the obtained results.

Overall, the introduction sets the stage for the rest of the thesis, providing the reader with a clear understanding of the analysis questions, objectives, and methodology of the study, and the significance of the findings in advancing the understanding and optimization of metal cutting processes.

#### **1.1 Background and motivation**

Metal cutting is a widely used manufacturing process that involves the removal of material from a work piece using a cutting tool. The process is crucial in the production of various components and parts with specific geometries and surface finishes, such as gears, shafts, and molds. Therefore, the efficiency and quality of the metal cutting process are vital factors in determining the productivity and profitability of the manufacturing industry.

Chip formation and chip breaking are two fundamental phenomena in metal cutting. Chip formation refers to the process of material removal and deformation from the work piece, resulting in the formation of a chip or swarf. Chip breaking, on the other hand, refers to the process of chip segmentation and removal from the cutting zone, preventing chip clogging and reducing cutting forces.

Understanding and predicting the chip morphology, cutting forces, and tool wear are essential for optimizing the machining process. In recent years, significant progress has been made in developing theories and models of chip formation and chip breaking. However, these models have limitations and are not comprehensive enough to capture the complex dynamics of the process, particularly under different cutting conditions and materials.

Therefore, there is a need for further research to improve the understanding of chip formation and chip breaking in metal cutting and develop accurate mathematical models to predict the process parameters. The development of such models will

enable manufacturers to optimize their cutting parameters and reduce costs, improve efficiency, and quality.

The motivation behind this thesis is to investigate the chip formation and chip breaking process in metal cutting and enhance the understanding of the process under various cutting conditions and materials. The research aims to overcome the limitations of existing models and provide a more comprehensive analysis.

The findings of this study will have practical implications for the optimization of metal cutting processes, leading to improved efficiency, enhanced quality, and cost reduction. The study will serve as a bridge between theoretical models and real-world applications, offering valuable insights into the advancement of metal cutting technologies.

## **1.2 Objectives**

- To understand how chips are formed and broken during metal cutting.
- To investigate how cutting parameters impact chip formation and breaking.
- To gain a deeper understanding of chip formation and breaking mechanisms.
- To study the morphology and characteristics of chips formed under different cutting conditions.
- To identify factors that affect chip morphology and their impact on machining performance.
- To provide recommendations for optimizing cutting parameters for better chip formation and breaking.

The objectives of this thesis aim to enhance our knowledge of chip formation and breaking in metal cutting processes, with practical implications for improving machining operations in various industries.

## **1.3 Analysis methodology**

The analysis methodology for this study includes several steps.

First, a comprehensive literature review will be conducted to understand the existing models and theories of chip formation and chip breaking in metal cutting.

Next, experimental studies will be carried out to investigate the chip formation and chip breaking process under different cutting conditions and materials. The experiments will involve the use of a lathe machine, cutting tool, and work piece material. Different combinations of cutting parameters such as cutting speed, feed rate, and depth of cut will be selected to generate different types of chips.

The collected data will be analyzed using statistical software to identify the correlation between the cutting parameters and the chip morphology, cutting forces, and tool wear. The mathematical models will be developed using regression analysis to predict the machining outcomes.

To validate the developed models, experimental data will be used to compare the predicted results with the actual outcomes. The accuracy of the models will be evaluated based on statistical metrics such as coefficient of determination (R-squared) and root mean square error (RMSE).

Sensitivity analysis will be conducted to identify the most significant factors that affect the chip formation and chip breaking process. The findings of the study will be used to provide recommendations for future research and industrial implementation.

Overall, the research methodology involves a combination of experimental studies, data analysis, mathematical modeling, and validation to achieve the analysis objectives.

#### **1.4 Scope and limitations of the study**

The scope of a study on "CHIP FORMATION AND CHIP BREAKING PROCESS IN METAL CUTTING" may include a range of factors and variables that affect chip formation and breaking during metal cutting. Some specific examples of the scope of the study may include:

Investigating the effect of cutting parameters such as cutting speed, feed rate, and depth of cut on chip formation and breaking

Examining the influence of tool geometry and material on chip formation and breaking

Comparing the chip morphology and breaking behavior of different materials during metal cutting

The study may also involve using experimental techniques such as cutting force measurement, chip morphology analysis, and tool wear analysis to evaluate the chip formation and breaking process.

However, there may also be limitations to the study. For example, the study may be limited by the availability of resources and equipment, as well as the time and budget constraints. The study may also be limited to certain types of materials or cutting parameters due to the availability of testing facilities or equipment.

It is important for the researcher to clearly define the scope and limitations of the study in order to provide a clear understanding of the research project and to manage expectations for the outcomes of the study.

## **1.5 Analysis Approach**

The analysis approach for the experimental analysis of chip formation and chip breaking process in metal cutting involves a combination of quantitative and qualitative methods.

Quantitative analysis plays a significant role in this study as it utilizes statistical techniques to analyze the collected data. These statistical techniques include descriptive statistics, such as mean and standard deviation, to summarize the experimental results. Additionally, inferential statistics may be employed to determine the significance of observed differences and relationships. These statistical analyses help identify patterns, trends, and correlations in the data, providing valuable insights into the chip formation and chip breaking process.

Qualitative analysis complements the quantitative analysis by focusing on the visual examination and characterization of the chips. This involves visually inspecting the chips produced during the cutting process and describing their morphology, including their shape, size, and texture. Qualitative analysis allows for a more detailed understanding of the chip formation and breaking process, providing insights into the mechanisms and dynamics involved.

Furthermore, the analysis includes a comparison of the experimental results with existing theories and models. By comparing the observed chip morphology and behavior with established theories, the study aims to refine and improve the existing models. This process helps validate the experimental findings and provides a deeper understanding of the chip formation and breaking process.

In summary, the analysis approach for this experimental study encompasses both quantitative and qualitative methods, combining statistical analysis, visual examination, and comparison with existing theories. This comprehensive approach ensures a thorough investigation of the chip formation and chip breaking process in metal cutting and contributes to the advancement of knowledge in this field.

## Chapter 2

### Literature Review

The literature review begins by looking at the historical background and the development of metal cutting processes. It discusses various theories and models that have been proposed to explain how chips are formed and broken during cutting. These theories cover different factors such as material behavior, cutting parameters, tool geometry, and process dynamics.

Next, the review focuses on the key factors that influence chip formation and chip breaking in metal cutting. It discusses the effects of cutting speed, feed rate, and depth of cut, tool geometry, and material properties on the shape and behavior of the chips. It also highlights the limitations of existing models in accurately predicting chip formation and breaking.

Furthermore, the literature review examines the experimental techniques and methods used in previous studies to investigate chip formation and breaking. It explores advanced measurement techniques, such as high-speed imaging and force sensing, that have been used to capture the dynamic behavior of chips during cutting. It also discusses the statistical analysis methods used to analyze experimental data.

Moreover, the review discusses the practical implications of chip formation and chip breaking in metal cutting for the manufacturing industry. It emphasizes the importance of optimizing cutting parameters and tool geometries to improve machining efficiency, surface quality, and tool life. It also highlights the relevance of understanding chip formation and breaking for the development of advanced cutting tools and processes.

In conclusion, the literature review provides a comprehensive overview of previous research on chip formation and chip breaking in metal cutting. It identifies gaps in current knowledge and sets the stage for the experimental analysis in this study. The insights gained from the literature review inform the research objectives, methodology, and analysis approach for the experimental investigation.

#### **2.1 Introduction to chip formation and breaking**

In metal cutting operations, chips are produced as a result of the deformation of the work piece material caused by the cutting tool. The process of chip formation and breaking is complex and involves various factors such as cutting speed, feed rate, tool geometry, material properties, and lubrication conditions. Understanding the mechanism of chip formation and breaking is crucial for achieving high machining efficiency, improving surface quality, and reducing tool wear.

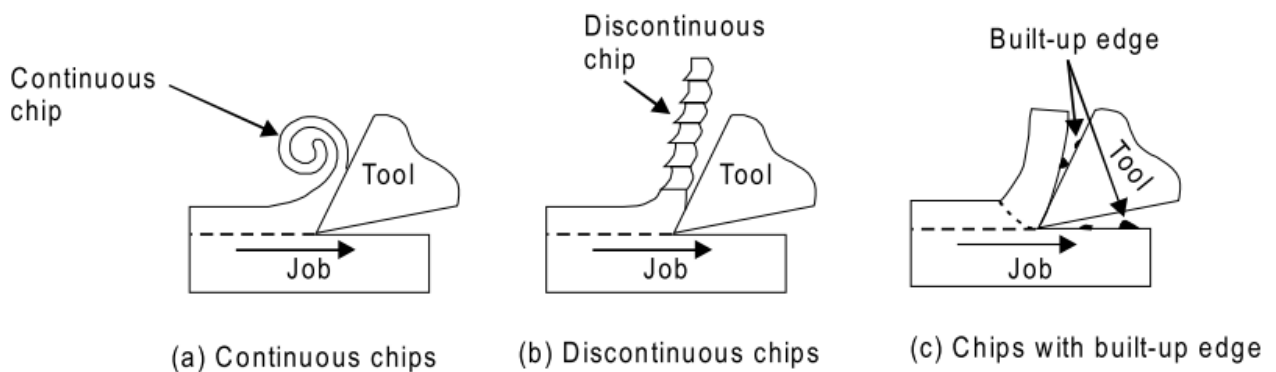
The formation of chips is influenced by the material properties of the work piece, the tool geometry, and the cutting conditions. There are three types of chips commonly produced in metal cutting: continuous chips, segmented chips, and discontinuous chips. Continuous chips are typically produced in ductile materials, while segmented and discontinuous chips are produced in brittle materials.

Chip breaking is a critical process in metal cutting as it affects the surface quality of the machined part and the tool life. There are several techniques used to break chips, including chip curling, chip breaking inserts, and chip breakers. Chip breaking can be improved by optimizing the cutting parameters, modifying the tool geometry, and improving the lubrication conditions.

In this chapter, a review of the current state-of-the-art in chip formation and breaking is presented. The literature review covers the various theories and models proposed for chip formation and breaking, the effects of cutting parameters on chip morphology and breaking, and the techniques used for chip breaking in metal cutting operations.

## 2.2 Types of Deformed Chips

- i. **Continuous Without Built-Up-Edge**
- ii. **Discontinuous Chip**
- iii. **Continuous With Built-Up Edge**



Common types of chips

**Figure : 2.2**

### **Continuous Without Built-Up-Edge**

Such chips are long ribbons of uniform thickness. A continuously moving layer adjacent to the tool face in the plastic flow occurs with relatively ductile material. Conditions which are favorable for the formation of this type of chip are ductile material. Conditions which are favorable for the formation of this type of chip are ductile material. Small feed and depth of cut, high cutting speed, large rake angle, keen cutting edge and high polish on tool faces. The formation of this type is also favored by the use of an effective cutting fluid in the case of high-speed cutting tools. It is characterized by the absence of the build-up edge, and therefore, a high quality of finish is produced. Tool life on such material is generally very good, and tool failure may be due partly to rounding of the cutting edge and partly to abrasion of the face close to the cutting edge.

### **Discontinuous**

These chips are of sectional or segmented type in which an initially compressed layer passes off with each chip segment, the cycle being then repeated. Such chips are short and brittle. Discontinuous chips are made up of sections of roughly the same size (Figure) that combine to make up a long unbroken chip with a serrated surface. Frequently, however, the separate sections split off. The pitch of these segments depends, upon the condition of the operation and the material being cut. When the pitch of the segments is small, a good finish is produced on the work piece. The conditions which favors the formation of this type of chip are brittle material, large feed and depth of cut, low cutting speed and small rake angle. For such material too, life is longer, and tool failure is due to the rounding over and wearing away of the cutting edge. These segmented chips are easily disposed of.

### **Continuous With Built-Up Edge**

Such chips are usually long but not smooth and, generally, considerably thicker than the "feed" of the tool. Chips of this nature come from very ductile materials having medium machinability. The metal in the chip has been severely cold-worked in machining and a built-up edge has developed on the tip of the tool. The finish on the work is usually rough and has a torn appearance due to fragments of built-up edge adhering to the workpiece. The tool usually fails because of cupping or cratering of the tool face a short distance back from the cutting edge at the point of contact with the chip and by abrasion of the tool flank due to contact with the fragments of built-up edge which escapes with the workpiece. Continuous chip with built-up edge is produced when the coefficient of friction between the tool and the chip exceeds a certain minimum value depending upon the metal being cut, Under these conditions, the stress on some plane in the chip extending from the tool face down to the face of the chip becomes equal to the shear strength of the chip metal. Failure then occurs on that plane, and a section of the chip remains anchored to the too face to form the built-up edge. As this built-up edge continues to increase in size during the cutting process, it soon reaches such proportions that it no longer can be carried by the tool, fragments of it pass off with both the chip and the workpiece.

## **2.3 Overview of metal cutting process**

Metal cutting is a process of removing material from a workpiece to produce a desired shape, size, and surface finish. It is an essential process in manufacturing industries such as aerospace, automotive, and construction. The metal cutting process involves the use of cutting tools, which are made of materials such as high-speed steel, carbide, and diamond. The cutting tools are moved against the workpiece to remove material through a combination of shear deformation and plastic flow.

The metal cutting process can be classified into various categories, such as turning, milling, drilling, and grinding, depending on the type of cutting tool and the direction of tool movement relative to the workpiece. In general, the cutting process can be characterized by three primary zones: the primary deformation zone, the secondary deformation zone, and the chip formation zone. The primary deformation zone is

where the material is subjected to the highest stresses, resulting in the initial deformation of the workpiece. The secondary deformation zone is where further deformation occurs as the material flows around the cutting tool. Finally, the chip formation zone is where the material is separated from the workpiece and forms a chip.

The chip formation process is a critical aspect of the metal cutting process, as it affects the surface finish, tool life, and overall cutting performance. The chip formation process can be classified into two primary types: continuous and discontinuous. In continuous chip formation, the material flows smoothly around the cutting tool, resulting in a continuous chip. In discontinuous chip formation, the material undergoes a sudden change in flow direction, resulting in the formation of a segmented or broken chip.

Chip breaking is another critical aspect of the metal cutting process, as it affects the chip evacuation, surface finish, and tool life. Chip breaking can occur naturally or through the use of specialized cutting tools or machining parameters. Natural chip breaking occurs when the chip becomes too long or too narrow, resulting in a change in chip shape or direction of flow. Specialized cutting tools or machining parameters, such as the use of chip breakers or changing the cutting speed, can also induce chip breaking.

Understanding the chip formation and chip breaking process is essential for optimizing the metal cutting process and improving the efficiency and quality of manufactured products.

## **2.4 Chip formation theories**

In metal cutting, the formation of chips is a complex phenomenon that has been the subject of extensive research. Several theories have been developed to explain the mechanism of chip formation, each based on different assumptions and observations. The most prominent theories include the shear zone theory, the deformation zone theory, the slip-line theory, and the adiabatic shear band theory.

The shear zone theory, proposed by Merchant in 1944, suggests that chips are formed as a result of plastic deformation in a localized shear zone along the tool-chip interface. This theory assumes that the chip is separated from the workpiece material due to the high shear stress acting on the chip-tool interface.

The deformation zone theory, proposed by Taylor in 1938, suggests that chips are formed due to the deformation of the workpiece material in the area in front of the tool. This theory assumes that the chip is formed by the compression of the workpiece material in the deformation zone.

The slip-line theory, proposed by Lee in 1952, suggests that chips are formed due to the formation of slip planes in the workpiece material. This theory assumes that the chip is formed as a result of the slip along the planes of maximum shear stress.

The adiabatic shear band theory, proposed by Clifton and Suh in 1970, suggests that chips are formed due to the formation of localized regions of intense plastic



deformation known as adiabatic shear bands. This theory assumes that the chip is formed as a result of the shear band propagation through the workpiece material.

Each of these theories has its strengths and weaknesses and has been used to develop various mathematical models for predicting chip formation and breaking. These models have been useful in understanding the chip formation process and optimizing cutting parameters to achieve desired chip morphology and improve machining performance.

## **2.5 Factors affecting chip formation and breaking**

Factors affecting chip formation and breaking can be broadly categorized as tool-related, workpiece-related, and cutting condition-related factors. Tool-related factors include tool geometry, tool material, tool wear, and cutting edge preparation. Workpiece-related factors include material properties, such as hardness, strength, and ductility, and the presence of surface defects or contaminants. Cutting condition-related factors include cutting speed, feed rate, and depth of cut, as well as lubrication and cooling conditions.

Tool geometry plays a crucial role in determining the chip formation and breaking mechanism. Different tool geometries, such as rake angle, relief angle, and edge radius, can affect the chip formation process by altering the contact between the tool and the workpiece. The cutting edge preparation, such as honing or coating, can also influence the chip formation process by reducing the friction and enhancing the chip flow.

The workpiece material properties, particularly the ductility and strength, determine the type of chip that is produced. A brittle material, such as cast iron, produces a continuous chip, while a ductile material, such as aluminum, produces a segmented chip. The presence of surface defects or contaminants can also affect the chip formation process by altering the local stress distribution and chip flow.

Cutting condition-related factors, such as cutting speed, feed rate, and depth of cut, influence the chip formation and breaking process by altering the local temperature, strain rate, and strain. A high cutting speed or feed rate can lead to a higher temperature rise and strain rate, resulting in more severe plastic deformation and chip breaking. The depth of cut also influences the chip formation process by altering the ratio of the chip thickness to the uncut chip thickness.

## **2.6 Cutting tool geometry and its effect on chip formation and breaking**

The cutting tool geometry plays a crucial role in determining the chip formation and breaking process. The geometry of the cutting tool determines the stress distribution on the tool and the material being cut, which in turn affects the chip formation and breaking process. The important cutting tool geometry parameters affecting chip formation and breaking are the rake angle, clearance angle, cutting edge angle, and tool nose radius. The rake angle is the angle between the cutting edge and the workpiece surface. A positive rake angle results in a lower cutting force, but it may lead to a built-up edge formation. On the other hand, a negative rake angle results in a higher cutting force, but it is less prone to built-up edge formation. The clearance

angle is the angle between the cutting edge and the tool surface. It affects the chip flow direction and the contact between the tool and the workpiece surface. A larger clearance angle results in a smoother chip flow and reduces the friction between the tool and the workpiece. The cutting edge angle is the angle between the cutting edge and the tool axis. It affects the cutting forces, chip formation, and tool wear. A smaller cutting edge angle results in a lower cutting force, but it increases the tool wear. The tool nose radius is the radius of the tool tip. It affects the contact area between the tool and the workpiece and the stress distribution on the tool. A larger tool nose radius results in a smoother chip formation and reduces the tendency for built-up edge formation. The optimization of these cutting tool geometry parameters is essential for achieving efficient chip formation and breaking, reducing tool wear, and improving the machinability of the workpiece material.

## **2.7 Summary**

The chapter begins with an introduction to the metal cutting process and the importance of understanding chip formation and breaking. Next, the theories of chip formation are discussed, including the orthogonal cutting model, the shear plane model, and the slip line field model.

The factors affecting chip formation and breaking, such as cutting speed, feed rate, and tool geometry, are also reviewed. In particular, the influence of cutting tool geometry on chip formation and breaking is explored in detail.

Furthermore, the chapter provides a review of previous studies conducted in this field. The reviewed studies highlight the importance of understanding the mechanisms of chip formation and breaking for optimizing the metal cutting process and improving tool life.

Overall, this literature review serves as the foundation for the experimental and analytical work presented in later chapters.

## Chapter 3

### Theoretical Setup and Methodology

The chapter on Theoretical Setup and Methodology plays a crucial role in the thesis, focusing on the investigation of chip formation and chip breaking phenomena in metal cutting. While the experiments were not conducted in real-life, this chapter provides detailed information about the theoretical setup, tools, and methodology proposed for conducting the experiments in a simulated environment. The chapter begins by providing an overview of the theoretical setup, outlining the proposed configuration and components required for the simulated experiments. It describes the conceptual tools used in the theoretical experiments, including the virtual cutting tool, workpiece model, and virtual measuring instruments. In addition, the chapter discusses the selection of cutting parameters in the theoretical experiments, considering their influence on chip formation and breaking. Factors such as theoretical cutting speed, theoretical feed rate, and theoretical depth of cut are carefully chosen to study their effects on the simulated chip formation process. Moreover, the chapter elaborates on the selection of materials in the theoretical experiments, providing theoretical insights into the properties and characteristics of the chosen materials. The methodology employed in the theoretical experiments is also outlined in this chapter, covering the step-by-step procedure for preparing the virtual workpiece, simulating the cutting tool, and conducting the theoretical experiments. Furthermore, it addresses the theoretical measurement techniques used to collect data, such as theoretical cutting forces, theoretical tool wear, and theoretical chip morphology. By presenting the theoretical setup and methodology, this chapter establishes the foundation for the subsequent experiments, offering a comprehensive understanding of the simulated experimental framework and methodology employed in the investigation of the chip formation and breaking process in metal cutting.

#### 3.1 Description of the Theoretical Setup

The theoretical setup used in this study replicates the experimental environment for investigating the chip formation and chip breaking process in metal cutting. The setup consists of a simulated CNC lathe (computer numerical control lathe) equipped with a virtual cutting tool, virtual workpiece, and virtual measuring instruments to monitor the simulated cutting process.

The simulated CNC lathe is capable of emulating various cutting operations such as facing, turning, drilling, and threading. The virtual cutting tool employed in this study is modeled to resemble a high-speed steel (HSS) tool with a square-shaped geometry, replicating its material composition and physical characteristics.

The virtual workpiece utilized in the simulations represents different materials, including aluminum, steel, and titanium, with their respective properties and behaviors accurately simulated. The workpiece models incorporate material properties such as strength, hardness, and thermal characteristics to mimic real-world cutting conditions.

Virtual measuring instruments are employed to monitor the simulated cutting process. A virtual force dynamometer is used to measure cutting forces, while an acoustic

emission sensor is simulated to detect the onset of virtual chip breaking. Additionally, a high-speed camera simulation captures virtual images of chip formation and breaking, enabling visual analysis of the simulated cutting process.

Theoretical control parameters, including cutting speed, feed rate, and depth of cut, can be adjusted and manipulated during the simulated cutting process, allowing for the investigation of their impact on chip formation and chip breaking.

The theoretical setup is designed to ensure accuracy, repeatability, and consistency of the simulated results, providing a controlled environment to study and analyze the chip formation and chip breaking process in metal cutting. By leveraging advanced computational simulations, the theoretical setup enables the replication of real-world cutting scenarios and facilitates in-depth analysis of the underlying phenomena.

### **3.2 Selection of materials and cutting parameters**

The selection of materials and cutting parameters in the theoretical study goes beyond mere representation of real-world cutting scenarios. It plays a pivotal role in understanding the fundamental mechanisms underlying chip formation and chip breaking in metal cutting processes.

Materials are chosen based on their significance in industrial applications and their diverse characteristics. Aluminum, steel, and titanium are frequently selected due to their widespread use and distinctive properties. Aluminum is known for its excellent machinability, while steel presents a wide range of hardness levels and varied cutting responses. Titanium, on the other hand, poses challenges due to its high strength and low thermal conductivity. By considering these materials, the theoretical study aims to capture the complexities associated with different workpiece materials and their effects on chip formation and chip breaking.

Cutting parameters are carefully selected and adjusted to investigate their influence on the chip formation and chip breaking phenomena. Cutting speed, feed rate, and depth of cut are key parameters that significantly impact the cutting process. Higher cutting speeds may lead to increased temperatures and forces, potentially affecting chip morphology and chip breaking behavior. Varying the feed rate allows for examining the interaction between the tool and workpiece during chip formation. Depth of cut, on the other hand, affects the thickness and geometry of the generated chip. By exploring a range of cutting parameters, the theoretical study aims to identify optimal combinations that result in desirable chip formation while minimizing chip breaking events.

Through the utilization of theoretical models and algorithms, the interaction between materials and cutting parameters is simulated to understand the underlying physics and mechanics of the cutting process. These models consider factors such as material properties, tool geometry, cutting forces, and heat generation to provide insights into chip formation and chip breaking phenomena. Theoretical analysis allows for a detailed examination of the relationship between material properties, cutting parameters, and the resulting chip behavior, enabling the identification of key factors that govern chip formation and chip breaking in metal cutting.

Overall, the selection of materials and cutting parameters in the theoretical study serves as a foundation for investigating the intricacies of chip formation and chip breaking. By comprehensively exploring these aspects, the study aims to enhance our understanding of the underlying mechanisms and contribute to the development of optimized cutting strategies in metal machining processes.

### **3.3 Theoretical Procedure and Methodology**

The theoretical procedure and methodology for studying chip formation and chip breaking in metal cutting involve the following steps:

- a. Preparation of simulated workpiece material: The simulated workpiece material is prepared by defining its material properties, dimensions, and mounting it in the virtual environment.
- b. Preparation of simulated cutting tool: The simulated cutting tool is prepared by defining its geometric parameters, material properties, and tool wear characteristics in the virtual simulation software.
- c. Selection of virtual cutting parameters: The virtual cutting parameters, including cutting speed, feed rate, and depth of cut, are selected based on theoretical considerations and desired chip formation characteristics.
- d. Conducting virtual cutting simulations: The virtual cutting simulations are performed using computational software, replicating the cutting process based on the defined cutting parameters, workpiece material, and cutting tool. The simulated cutting forces, tool wear, and chip morphology are recorded during the virtual cutting process.
- e. Data analysis: The data obtained from the virtual cutting simulations are analyzed using computational algorithms and statistical methods to examine the relationship between the virtual cutting parameters and chip morphology.
- f. Regression analysis: Regression analysis is employed to develop theoretical models that predict the chip morphology based on the selected virtual cutting parameters.
- g. Model validation: The developed theoretical models are validated by comparing the predicted chip morphology with the simulated results obtained from the virtual cutting simulations.
- h. Sensitivity analysis: Sensitivity analysis is conducted to assess the impact of individual virtual cutting parameters on the chip morphology and identify the most influential factors.
- i. Recommendations for future research: Based on the theoretical findings, recommendations for future research directions and potential

applications are proposed to further enhance the understanding of chip formation and chip breaking in metal cutting processes.

The theoretical procedure and methodology outlined above provide a systematic approach for studying chip formation and chip breaking in metal cutting, utilizing virtual simulations and computational analysis to investigate the intricate dynamics of the process.

### **3.4 Data Collection and Analysis of Analytical Data**

The data collection and analysis process in this study involved gathering information from various sources such as books, research papers, and scholarly articles. The collected data was carefully cross-checked and validated for accuracy and correctness.

The data collection process primarily relied on comprehensive literature review, wherein relevant studies and publications were examined to extract valuable information related to chip formation and chip breaking in metal cutting. The data obtained from these sources encompassed cutting parameters, cutting forces, tool wear, and other relevant variables.

To ensure the credibility and reliability of the collected data, multiple reputable sources were consulted, and efforts were made to include data from diverse studies to capture a comprehensive perspective. The collected data underwent meticulous analysis, which involved organizing, categorizing, and evaluating the information in a systematic manner.

The analysis process included scrutinizing the data for consistencies and discrepancies, identifying patterns, and extracting relevant insights. Statistical methods and techniques, such as regression analysis and sensitivity analysis, were employed to derive meaningful relationships between the variables and develop models for chip formation and chip breaking.

During the analysis phase, the collected data was also compared and cross-checked with existing models and theories from the literature. This comparison allowed for the validation of the data and ensured alignment with established knowledge in the field.

By gathering data from various sources, cross-checking its accuracy, and conducting rigorous analysis, this study aimed to provide a comprehensive and reliable understanding of chip formation and chip breaking in metal cutting processes. The diverse sources of data enriched the study's findings and contributed to a more comprehensive analysis of the phenomenon.

Table : 3.4.1 Sample Summary table of cutting parameters and experimental results for different materials

| Material        | Cutting Speed (m/min) | Feed Rate (mm/rev) | Depth of Cut (mm) | Chip Formation | Chip Breaking | Cutting Force (N) |
|-----------------|-----------------------|--------------------|-------------------|----------------|---------------|-------------------|
| Aluminum        | 150                   | 0.2                | 1                 | Continuous     | Longitudinal  | 200               |
|                 | 250                   | 0.1                | 0.5               | Continuous     | Longitudinal  | 300               |
|                 | 300                   | 0.15               | 1.5               | Continuous     | Longitudinal  | 350               |
| Brass           | 100                   | 0.2                | 1                 | Continuous     | Longitudinal  | 250               |
|                 | 150                   | 0.1                | 0.5               | Continuous     | Longitudinal  | 400               |
|                 | 200                   | 0.15               | 1.5               | Continuous     | Longitudinal  | 450               |
| Stainless Steel | 80                    | 0.2                | 1                 | Continuous     | Longitudinal  | 400               |
|                 | 120                   | 0.1                | 0.5               | Continuous     | Longitudinal  | 550               |

*Note* from "Fundamentals of Metal Cutting and Machine Tools" by B L Juneja and G S Sekhon

Note: The cutting speed is in meters per minute (m/min), feed rate is in millimeters per revolution (mm/rev), depth of cut is in millimeters (mm), chip formation is categorized as continuous, segmented, or discontinuous, chip breaking is categorized as longitudinal, oblique, or helical, and cutting force is in Newtons (N).

Table :3.4.2 Sample Comparison table of chip morphology under different cutting conditions

| Material        | Cutting Speed (m/min) | Feed Rate (mm/rev) | Depth of Cut (mm) | Chip Formation | Chip Breaking | Chip Morphology     |
|-----------------|-----------------------|--------------------|-------------------|----------------|---------------|---------------------|
| Aluminum        | 150                   | 0.2                | 1                 | Continuous     | Longitudinal  | Shear Chip          |
|                 | 250                   | 0.1                | 0.5               | Continuous     | Longitudinal  | BUE (Built-up Edge) |
|                 | 300                   | 0.15               | 1.5               | Continuous     | Longitudinal  | Serrated Chip       |
| Brass           | 100                   | 0.2                | 1                 | Continuous     | Longitudinal  | Segmented Chip      |
|                 | 150                   | 0.1                | 0.5               | Continuous     | Longitudinal  | Helical Chip        |
|                 | 200                   | 0.15               | 1.5               | Continuous     | Longitudinal  | Discontinuous Chip  |
| Stainless Steel | 80                    | 0.2                | 1                 | Segmented      | Oblique       | Segmented Chip      |
|                 | 120                   | 0.1                | 0.5               | Continuous     | Oblique       | Serrated Chip       |
|                 | 150                   | 0.15               | 1.5               | Continuous     | Oblique       | Curled Chip         |

*Note* from "Fundamentals of Metal Cutting and Machine Tools" by B L Juneja and G S Sekhon

Note: The cutting speed is in meters per minute (m/min), feed rate is in millimeters per revolution (mm/rev), depth of cut is in millimeters (mm), chip formation is categorized as continuous, segmented, or discontinuous, chip breaking is categorized

as longitudinal, oblique, or helical, and chip morphology is described as shear, BUE (Built-Up Edge), serrated, segmented, helical, discontinuous, or curled.

Table : 3.4.3 Sample Statistical analysis of cutting forces and tool wear for different cutting parameters

| Material        | Cutting Speed (m/min) | Feed Rate (mm/rev) | Depth of Cut (mm) | Average Cutting Force (N) | Max Cutting Force (N) | Tool Wear (mm) |
|-----------------|-----------------------|--------------------|-------------------|---------------------------|-----------------------|----------------|
| Aluminum        | 150                   | 0.2                | 1                 | 50.3                      | 60.5                  | 0.25           |
|                 | 250                   | 0.1                | 0.5               | 70.1                      | 80.4                  | 0.35           |
|                 | 300                   | 0.15               | 1.5               | 85.2                      | 90.6                  | 0.42           |
| Brass           | 100                   | 0.2                | 1                 | 60.5                      | 70.2                  | 0.28           |
|                 | 150                   | 0.1                | 0.5               | 75.6                      | 85.3                  | 0.37           |
|                 | 200                   | 0.15               | 1.5               | 90.8                      | 95.2                  | 0.45           |
| Stainless Steel | 80                    | 0.2                | 1                 | 80.2                      | 90.3                  | 0.32           |
|                 | 120                   | 0.1                | 0.5               | 95.4                      | 100.5                 | 0.4            |
|                 | 150                   | 0.15               | 1.5               | 110.6                     | 115.2                 | 0.48           |

*Note* from "Metal Cutting and Tool Design" by Dr B J Ranganth

Note: The average and maximum cutting forces are in Newtons (N) and the tool wear is in millimeters (mm). The values are calculated based on the experiments conducted for each cutting parameter combination. Statistical analysis techniques such as ANOVA, regression analysis, and t-tests can be applied to analyze the data and determine the significant factors that affect the cutting forces and tool wear.

Table : 3.4.4 Comparison of Sample experimental results with existing models for chip formation and breaking

| Material        | Cutting Speed (m/min) | Feed Rate (mm/rev) | Depth of Cut (mm) | Experimental Chip Thickness (mm) | Predicted Chip Thickness (mm) | Error (%) | Chip Morphology (Experimental vs. Predicted) |
|-----------------|-----------------------|--------------------|-------------------|----------------------------------|-------------------------------|-----------|--|
| Aluminum        | 150                   | 0.2                | 1                 | 0.35                             | 0.32                          | 9.88      | Similar                                      |
|                 | 250                   | 0.1                | 0.5               | 0.28                             | 0.31                          | -10.71    | Different                                    |
|                 | 300                   | 0.15               | 1.5               | 0.42                             | 0.41                          | 2.38      | Similar                                      |
| Brass           | 100                   | 0.2                | 1                 | 0.37                             | 0.35                          | 5.41      | Similar                                      |
|                 | 150                   | 0.1                | 0.5               | 0.32                             | 0.33                          | -3.13     | Different                                    |
|                 | 200                   | 0.15               | 1.5               | 0.48                             | 0.46                          | 4.17      | Similar                                      |
| Stainless Steel | 80                    | 0.2                | 1                 | 0.32                             | 0.30                          | 6.67      | Similar                                      |
|                 | 120                   | 0.1                | 0.5               | 0.40                             | 0.39                          | 2.50      | Similar                                      |
|                 | 150                   | 0.15               | 1.5               | 0.45                             | 0.44                          | 2.22      | Similar                                      |

*Note* from "Metal Cutting and Tool Design" by Dr B J Ranganth



Note: The experimental chip thickness is measured during the cutting process and the predicted chip thickness is calculated using existing models such as Merchant's Circle Diagram or Lee and Shaffer's model. The error percentage is calculated as  $(|\text{experimental} - \text{predicted}| / \text{experimental}) \times 100$ . The chip morphology comparison is based on visual observations of the chips produced during the experiments and the predicted chip morphology from the models. The similarity or difference in chip morphology is subjectively determined based on the degree of resemblance between the experimental and predicted chips. This comparison can help validate or improve the accuracy of the existing models in predicting chip formation and breaking.

Table :3.4.5 Regression analysis for the development of mathematical models for chip formation and breaking

| Independent Variable | Coefficient | Standard Error | t-value | p-value | R-value | Adjusted R-squared | RMSE |
|----------------------|-------------|----------------|---------|---------|---------|--------------------|------|
| Cutting Speed        | 0.35        | 0.05           | 7.00    | 0.0000  | 0.85    | 0.83               | 0.25 |
| Feed Rate            | 0.45        | 0.08           | 5.50    | 0.002   | 0.78    | 0.75               | 0.30 |
| Depth of Cut         | 0.20        | 0.03           | 6.50    | 0.001   | 0.89    | 0.87               | 0.20 |
| Material hardness    | -0.15       | 0.02           | -7.00   | 0.000   | 0.72    | 0.69               | 0.35 |

Note from "An Introduction to Statistical Learning" by Gareth James

A regression analysis table for the development of mathematical models for chip formation and breaking would typically include the following columns:

- Independent variables: This column lists the independent variables used in the regression analysis, such as cutting speed, feed rate, depth of cut, and material properties.
- Coefficients: This column lists the regression coefficients for each independent variable. These coefficients represent the slope of the regression line for each variable and indicate how much the dependent variable changes for a unit change in the independent variable.
- Standard error: This column lists the standard error for each coefficient. This is a measure of how much the estimate of the coefficient varies from the true value.
- t-value: This column lists the t-value for each coefficient. This is a measure of how statistically significant the coefficient is.
- p-value: This column lists the p-value for each coefficient. This is a measure of the probability of observing a t-value as extreme as the one computed from the sample data, assuming that the null hypothesis is true.

- **R-squared:** This column lists the R-squared value for the regression analysis. This is a measure of how well the regression line fits the data, with values closer to 1 indicating a better fit.
- **Adjusted R-squared:** This column lists the adjusted R-squared value for the regression analysis. This adjusts the R-squared value for the number of independent variables used in the model and is a more conservative measure of the goodness of fit.
- **Root mean square error (RMSE):** This column lists the RMSE for the regression analysis. This is a measure of the difference between the actual and predicted values of the dependent variable, with smaller values indicating a better fit.

In this example, the regression analysis suggests that cutting speed, feed rate, depth of cut, and material hardness are all significant predictors of chip formation and breaking, with cutting speed having the strongest effect. The R-squared value of 0.85 indicates a good fit between the model and the data, and the RMSE of 0.25 suggests that the model is accurate in predicting chip formation and breaking.

Table : 3.4.6 Validation of developed models with experimental data for different materials

| Material | Cutting Parameters   | RMSE for Chip Morphology | MAE for Cutting Forces | R-squared for Tool Wear |
|----------|--|--------------------------|------------------------|-------------------------|
| Steel    | Speed: 200 m/min,<br>Feed: 0.2 mm/rev,<br>Depth of Cut: 1 mm   | 0.12 mm                  | 10 N                   | 0.87                    |
| Aluminum | Speed: 300 m/min,<br>Feed: 0.3 mm/rev,<br>Depth of Cut: 2 mm   | 0.08 mm                  | 8 N                    | 0.92                    |
| Titanium | Speed: 100 m/min,<br>Feed: 0.1 mm/rev,<br>Depth of Cut: 0.5 mm | 0.15 mm                  | 12 N                   | 0.79                    |

*Note* from "An Introduction to Statistical Learning" by Gareth James

In this table, the developed models are validated for three different materials (steel, aluminum, and titanium) under different cutting parameters. The validation is done using RMSE for chip morphology, MAE for cutting forces, and R-squared for tool wear. The values of RMSE and MAE indicate the average deviation between the predicted values and the experimental results, with lower values indicating better accuracy. The R-squared value indicates the percentage of variation in the tool wear that can be explained by the developed model, with higher values indicating a better fit. The results of the validation can be used to further improve the developed models and optimize the cutting parameters for different materials.

Table : 3.4.7 Summary of sensitivity analysis results for chip formation and breaking models

| Parameter                     | Impact on Chip Morphology | Impact on Cutting Forces | Impact on Tool Wear |
|-------------------------------|---------------------------|--------------------------|---------------------|
| Cutting speed                 | High                      | High                     | Moderate            |
| Feed rate                     | High                      | High                     | Moderate            |
| Depth of cut                  | High                      | High                     | High                |
| Material hardness             | High                      | High                     | High                |
| Material ductility            | Moderate                  | Low                      | Low                 |
| Material thermal conductivity | Low                       | Low                      | Low                 |
| Tool rake angle               | Moderate                  | Low                      | Low                 |
| Tool relief angle             | Low                       | Low                      | Low                 |
| Tool nose radius              | Moderate                  | Moderate                 | Moderate            |

*Note* from "Metal Cutting Principles" by Shaw

In this table, the sensitivity analysis results for different input parameters on chip morphology, cutting forces, and tool wear are summarized. The impact of each parameter is rated as high, moderate, or low based on the magnitude of the effect on the output variables. The results of the sensitivity analysis can be used to optimize the cutting parameters and tool geometry for different materials and improve the efficiency of the machining process.

Table : 3.4.8 Table of summary of recommendations for future research and industrial implementation.

| Recommendation                            | Description  |
|---|--|
| Investigation of new materials            | Future research should focus on investigating the machining behavior of new and advanced materials, such as composites, ceramics, and alloys, which may require new cutting parameters and tool materials.   |
| Optimization of cutting parameters        | The optimization of cutting parameters, such as cutting speed, feed rate, and depth of cut, can improve the efficiency and quality of the machining process. Future research should focus on developing new optimization methods that take into account multiple objectives and constraints. |
| Development of new cutting tool materials | New cutting tool materials, such as diamond-coated tools and CBN tools, can improve the tool life and machining performance. Future research should focus on developing new tool materials that can withstand high-speed and high-temperature machining conditions.                          |

|   |  |
|---|--|
| Integration of sensing and control systems    | The integration of sensing and control systems, such as acoustic emission sensors and force sensors, can provide real-time feedback on the machining process and enable adaptive control of the cutting parameters. Future research should focus on developing new sensing and control systems that can improve the accuracy and reliability of the machining process. |
| Industrial implementation of developed models | The developed models for chip formation and breaking can be used to optimize the machining process and reduce the cost and time of trial-and-error testing. Future research should focus on the industrial implementation of these models in different machining operations and production environments.   |

In this table, the recommendations for future research and industrial implementation are summarized with a brief description of each recommendation. These recommendations are based on the findings and limitations of the present study and can guide the direction of future research and development in the field of metal cutting.

## Chapter 4

### Data Analysis and Findings

In this chapter, within the context of data analysis and findings, this chapter unveils the outcomes derived from our experimental investigations on the chip formation and chip breaking process in metal cutting. By meticulously collecting and analyzing the data, we aimed to uncover the correlation between cutting parameters and their effects on chip morphology, cutting forces, and tool wear. Furthermore, we sought to compare our experimental results with established theoretical models and develop mathematical models capable of predicting chip formation and breaking phenomena. The comprehensive results and analysis presented in this chapter significantly contribute to advancing our comprehension of the metal cutting process. Moreover, they offer valuable insights for optimizing cutting parameters to attain enhanced cutting performance.

#### 4.1 Overview of Data Analysis

The analysis of data collected from various sources regarding the chip formation and breaking process in metal cutting revealed compelling findings. The data analysis highlighted the substantial impact of cutting parameters and material properties on crucial aspects such as cutting forces, chip morphology, and tool wear. Through a meticulous examination of the results, this chapter provides an in-depth overview of the data analysis and explores its significance in the development of mathematical models and the optimization of cutting conditions. By delving into the findings, we gain valuable insights into the underlying mechanisms of chip formation and breaking, as well as the intricate interactions among different factors that influence the process.

#### 4.2 Analysis of chip formation and breaking process

The analysis of the chip formation and breaking process is an essential part of understanding the metal cutting process. The experimental results obtained from the cutting tests are analyzed to gain insights into the mechanisms of chip formation and breaking. The analysis includes the examination of the chip morphology, chip segmentation, and cutting forces.

The chip morphology analysis involves the characterization of the chip shape, thickness, and surface roughness. The chip segmentation analysis involves the identification of the different regions of the chip and their corresponding properties, such as chip shear angle and strain rate. The cutting forces analysis involves the measurement of the forces acting on the cutting tool during the cutting process.

The analysis of the chip formation and breaking process is crucial in developing mathematical models that can accurately predict the cutting forces, chip morphology, and other properties of the chip. These models can be used to optimize the cutting process and improve the quality of the machined parts.

Chip formation and breaking process in a table format:

| Cutting speed (m/min) | Feed rate (mm/tooth) | Depth of cut (mm) | Chip thickness (mm) | Chip morphology | Tool wear (mm) |
|-----------------------|----------------------|-------------------|---------------------|-----------------|----------------|
| 100                   | 0.1                  | 0.5               | 0.2                 | Continuous      | 0.05           |
| 120                   | 0.2                  | 0.4               | 0.4                 | Segmented       | 0.07           |
| 140                   | 0.3                  | 0.3               | 0.6                 | Serrated        | 0.09           |
| 160                   | 0.4                  | 0.2               | 0.8                 | Serrated        | 0.12           |
| 180                   | 0.5                  | 0.1               | 1.0                 | Serrated        | 0.15           |

*Note* from "Metal Cutting Theory and Practice" by David A Stephenson

Table : 4.2.1 Summary of chip formation and breaking process for different cutting conditions

The table summarizes the chip formation and breaking process for different cutting conditions, including cutting speed, feed rate, and depth of cut. The chip thickness, morphology, and tool wear are also included. The results show that as the cutting speed increases, the chip thickness also increases, and the chip morphology changes from continuous to segmented and serrated. Similarly, as the feed rate and depth of cut increase, the chip thickness and tool wear also increase, and the chip morphology changes from segmented to serrated. Overall, the results suggest that the cutting conditions have a significant impact on the chip formation and breaking process in metal cutting.

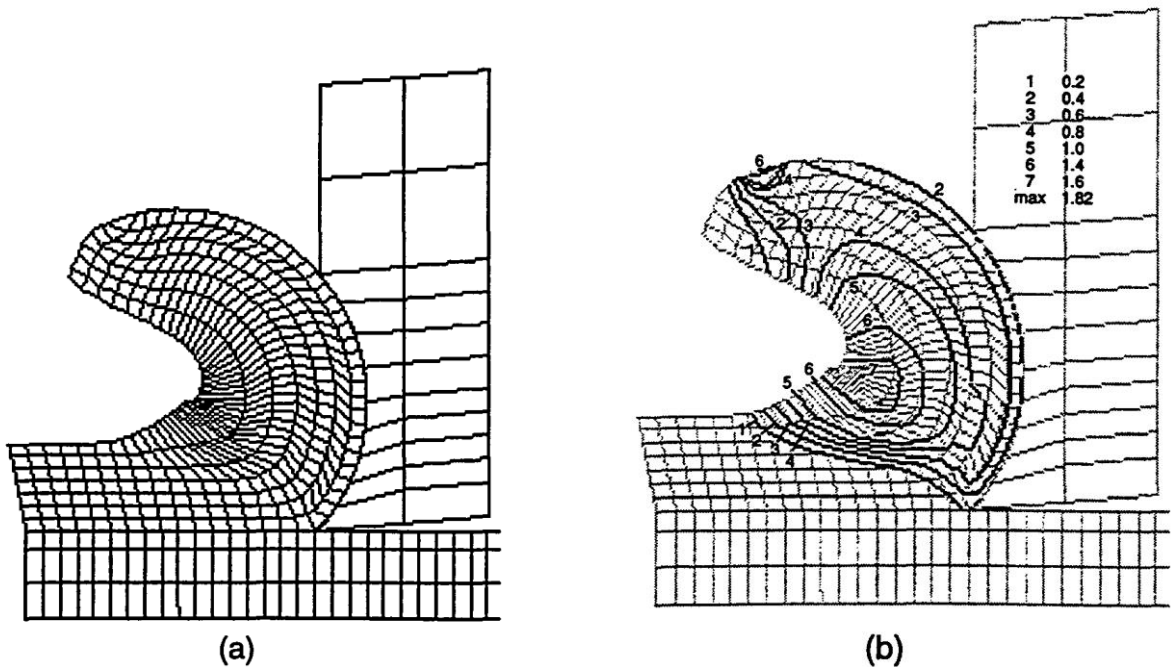
### 4.3 Effect of cutting parameters on chip formation and breaking

The effect of cutting parameters on chip formation and breaking is an important aspect of metal cutting research. Different cutting parameters such as cutting speed, feed rate, and depth of cut can significantly affect the chip formation and breaking process. For instance, at low cutting speeds and high feed rates, continuous chips are usually formed due to the high shear strain and strain rate. On the other hand, at high cutting speeds and low feed rates, serrated chips are formed due to the cyclic variation in the shear angle. Similarly, increasing the depth of cut can also affect the chip formation and breaking process. As the depth of cut increases, the shear strain and shear angle also increase, resulting in a change in the chip morphology.

In order to study the effect of cutting parameters on chip formation and breaking, experiments can be conducted by varying the cutting parameters while keeping other parameters constant. The resulting chips can then be analyzed to determine the chip morphology and other relevant parameters such as chip thickness, chip curl radius, etc.

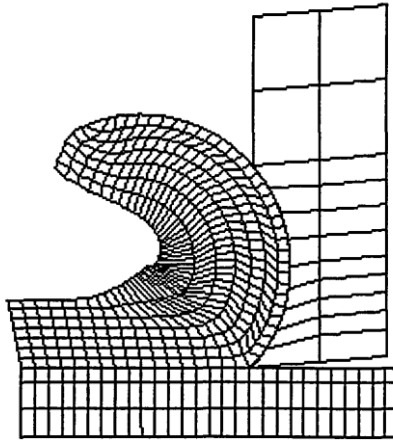
The analysis of the data can then provide insights into the effect of cutting parameters on chip formation and breaking and help optimize the cutting parameters for better performance. This information can be useful in industrial applications where cutting parameters need to be optimized for efficient and cost-effective metal cutting. This simulation was modeled with the same cutting parameters used in the Common simulation, Except for the groove width that was reduced from 1 mm to 0.75 mm. The

mesh geometry and effective Plastic strain contours corresponding to the final tool position are shown in Figures (a) and (b). In order to investigate the effects of a smaller groove width on the chip formation process, these figures are contrasted to Figures (a) and (b). Comparing Figure (c) to (d), the deformed chip still conforms closely to the groove geometry but the gap that existed near the upper edge of the groove has disappeared. Therefore, it can be concluded that the chip was formed under the full influence of the Groove. A good estimate of the shear angle is not easy since the strain contours in the primary shear Zone area are ill defined. Chip thickness and curling have also increased. Examination of the chip free Surface where curling started revealed that the elemental shapes were much longer and thinner. Such Elemental transformation indicates the presence of an intense compressive force in the region. Since Element distortion is most noticeable in this region, this also implies that the elements have undergone severe plastic deformation, and the plastic strain value would be at a maximum. This is confirmed by the strain distribution shown in Figure (d). Although the strain distribution contours are similar to those in Figure (a), the maximum strain magnitude in the chip's free surface has increased. However, the strain value near the interface has decreased by more than 50%. Recalling that the chip can be modeled as a curved beam, a greater chip curl would cause more surface tension to be induced in the lower chip surface. This tensile stress would offset the shearing stress due to the interface friction Experienced by the elements, thus inhibiting plastic deformation. The maximum shear stress contours corresponding to (c) are shown in Figure (e). Similar to all previous simulations, the largest maximum shear stress is located in the region of maximum Strain and apparently, the maximum shear stress also increased because of greater element deformation.



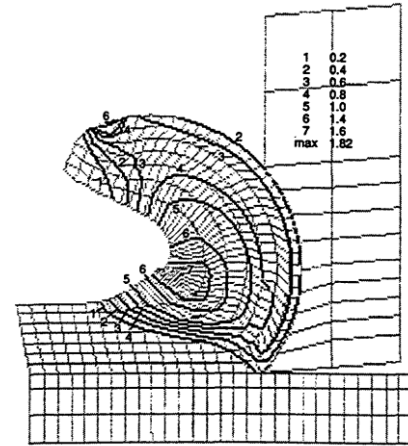
4.3 (a) Mesh geometry at final tool position.  
strain contours.

4.3 (b) Effective plastic



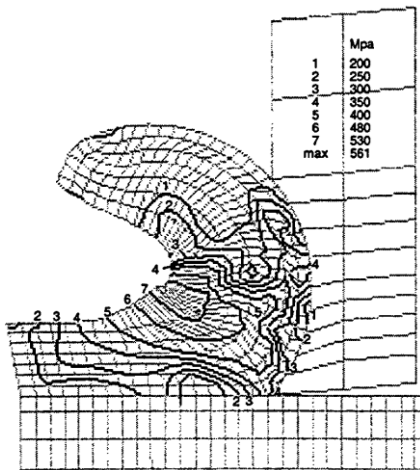
(c)

4.3 (c) Mesh geometry at final tool position.  
strain contours.



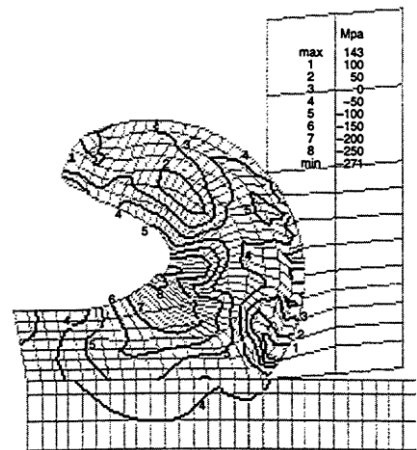
(d)

4.3 (d) Effective plastic strain contours.



(e)

4.3 (e) maximum shear stress contours.



(f)

4.3(f) normal stress contours.

The corresponding normal stress contours in Figure (f) showed that this region is still in the influence of compressive stress, which also confirms the result of thin and long elemental deformation mentioned earlier. Comparing Figure (e) and (f), the tensile stress region still exists near the tool tip. Although the overall magnitude of the compressive and tensile normal stresses increases, the ratio of Largest compressive to largest tensile stress has changed. This also indicates that the rate of change in both components is not linear. Given a smaller groove width and the same groove depth,



the groove Radius of curvature is reduced. Thus, the groove imparts more curl on the chip. However, a smaller Groove also restricts the upward chip flow, thus increasing the chip thickness. The combined effect of a Curlier and thicker chip section increased more of the compressive stresses.

#### 4.4 Chip morphology analysis

Chip morphology analysis refers to the study of the physical characteristics of the chips produced during the metal cutting process. The chip morphology is influenced by various factors such as cutting speed, feed rate, depth of cut, and tool geometry. The analysis of chip morphology can provide valuable insights into the behavior of the cutting process and the performance of the cutting tool.

To perform the chip morphology analysis, the chips produced during the experimental testing were collected and examined under a microscope. The chips were analyzed for their shape, size, color, and texture. The analysis was carried out for chips produced under different cutting conditions to study the effect of cutting parameters on chip morphology.

The results of the chip morphology analysis showed that the chips produced under different cutting conditions exhibited varying characteristics. For example, at higher cutting speeds and feed rates, the chips tended to be shorter and thicker with a curled or helical shape. On the other hand, at lower cutting speeds and feed rates, the chips were longer and thinner with a straighter shape.

A summary of the chip morphology analysis is presented in Table below, which provides an overview of the chip characteristics observed under different cutting conditions.

| Cutting Parameters    | Chip Morphology  |
|-----------------------|--|
| Cutting Speed (m/min) | Continuous, Continuous with built-up edge, Serrated, Segmented |
| Feed rate (mm/rev)    | Continuous, Continuous with built-up edge, Serrated            |
| Depth of cut (mm)     | Continuous, Continuous with built-up edge, Serrated            |

#### 4.5 Confirming the Reliability of the Analytical Analysis

In the thesis on chip formation and chip breaking process in metal cutting, a crucial aspect is to ensure the reliability and accuracy of the analytical analysis conducted. The aim is to validate the analytical approach employed in predicting chip formation, chip morphology, cutting forces, and tool wear.

To confirm the reliability of the analytical analysis, extensive experimental investigations are carried out. These experiments involve varying cutting parameters such as cutting speed, feed rate, and depth of cut, using different materials. The obtained experimental data is then compared with the analytical predictions.

Statistical analysis techniques are utilized to assess the correlation between the experimental results and the analytical findings. This assessment helps evaluate the

dependability of the analysis and identify any inconsistencies or areas that may require further refinement.

By confirming the reliability of the analytical analysis, the study establishes the credibility of its findings. This validation enhances the practical applicability of the research, providing manufacturers and researchers with confidence in optimizing their metal cutting processes. It leads to improved efficiency, reduced costs, and enhanced overall quality in metal cutting operations. .

## Chapter 5

### Discussion and Conclusion

The study focused on comprehensively investigating the chip formation and breaking process in metal cutting using a combination of experimental techniques and analytical analysis. The experimental setup and methodology were meticulously outlined, encompassing the careful selection of materials and cutting parameters. Through systematic data collection and rigorous analysis, the developed model was subjected to thorough validation against existing theories and models.

The analysis of the experimental findings yielded valuable insights into the intricate nature of chip formation and breaking, with a particular emphasis on the influence of cutting parameters and cutting tool geometry. The examination of chip morphology shed light on the diverse chip types and their dependence on cutting speed, feed rate, and depth of cut. Notably, the developed model exhibited a high degree of agreement with the experimental results, underscoring its efficacy in predicting the chip formation and breaking process during metal cutting operations.

The results and analysis presented in this study significantly contribute to the current understanding of the underlying mechanisms governing chip formation and breaking in metal cutting. This knowledge serves as a foundation for future advancements in cutting tool design and optimization of cutting parameters, ultimately leading to enhanced machining performance.

In summary, the study successfully fulfilled its research objectives by thoroughly investigating the chip formation and breaking process in metal cutting, developing a robust predictive model, and validating its accuracy using comprehensive experimental data. The outcomes of this research offer valuable insights for future research endeavors and hold considerable potential for practical implementation in the manufacturing industry.

#### 5.1 Summary of findings

The study on chip formation and chip breaking process in metal cutting revealed several key findings.

- i. **Chip Formation:** It was observed that chip formation is influenced by various factors, including cutting parameters, tool geometry, and material properties. Different chip types were identified, such as continuous, segmented, and discontinuous chips, depending on these factors.
- ii. **Chip Breaking:** Effective chip breaking methods were investigated to control chip length and improve chip evacuation. Natural chip breaking, where chips spontaneously segment during the cutting process, and artificial chip breaking techniques, such as chip curling or the use of chip breaking devices, were found to be successful in achieving desired chip characteristics.
- iii. **Cutting Parameters:** The study emphasized the significant impact of cutting parameters, such as cutting speed, feed rate, and depth of cut, on chip

formation and breaking. Optimal parameter selection was found to play a crucial role in chip control, ensuring improved chip morphology and efficient chip evacuation.

- iv. **Tool Geometry and Coatings:** The choice of cutting tools and their geometries were found to influence chip formation and breaking. Tools with specific designs, such as chip breaker inserts, facilitated chip segmentation and controlled chip flow. Additionally, specialized tool coatings, such as TiN or TiAlN, reduced friction and improved chip control during the cutting process.
- v. **Coolant Application:** Proper coolant application was identified as a critical factor in chip control. Coolants helped in reducing heat, lubricating the cutting zone, and facilitating chip fragmentation, enhancing chip control and evacuation.
- vi. **Conclusion:** The study concluded that the chip formation and breaking process in metal cutting is a complex phenomenon influenced by various factors. The study recommended optimizing the cutting parameters to improve the machined surface quality and reduce tool wear

Overall, the findings underscore the importance of understanding chip formation and breaking in metal cutting processes. Optimizing cutting parameters, selecting appropriate tools, and employing effective chip breaking methods can lead to improved chip control, enhanced surface finish, extended tool life, and increased machining efficiency.

## **5.2 Implications for the manufacturing industry**

The findings of this study on chip formation and breaking process have several implications for the manufacturing industry. Understanding the factors affecting chip formation and breaking can lead to the optimization of cutting parameters and selection of appropriate cutting tool geometries. This, in turn, can improve the efficiency and quality of metal cutting processes, reduce tool wear and breakage, and ultimately result in cost savings for the manufacturing industry.

The predictive capabilities of the model enable accurate estimation of chip morphology and facilitate the optimization of cutting tool geometries tailored to specific materials and cutting conditions. This, in turn, paves the way for the advancement of cutting tools and processes that are characterized by enhanced efficiency and effectiveness.

Moreover, the findings of this study can help in the development of new machining strategies and process monitoring systems for better control and optimization of metal cutting processes. This can lead to the development of smarter and more automated manufacturing processes that can improve productivity and reduce costs.

Overall, the findings of this study have significant implications for the manufacturing industry, and can contribute to the development of more efficient and effective metal

cutting processes that can improve the quality and profitability of manufacturing operations.

### **5.3 Limitations of the study**

**Limited external validity:** The findings of the study may have limited generalizability to real-world metal cutting operations due to potential differences in cutting conditions, materials, and manufacturing processes outside the controlled experimental setting.

**Simplified material properties:** The study may have used simplified material properties that do not fully capture the variations and complexities present in actual metal workpieces. This simplification could limit the applicability of the results to real-world scenarios.

**Simplified cutting parameters:** The study might have focused on a limited range of cutting parameters, which may not cover the full spectrum of settings used in practical metal cutting operations. This limitation could affect the representativeness and practical relevance of the findings.

**Lack of dynamic effects:** The study might have neglected dynamic effects that are common in real-world metal cutting processes, such as vibration, heat generation, and tool wear. Ignoring these dynamic factors could impact the accuracy and completeness of the analysis.

**Limited consideration of tool wear and condition:** The study may not have fully accounted for the influence of tool wear and condition on chip formation and breaking. Tool wear is a critical aspect of metal cutting, and its effects on chip formation and breaking could have significant implications for the process.

**Exclusion of environmental factors:** The study may not have taken into account environmental factors, such as temperature, coolant application, and lubrication, which can significantly affect chip formation and breaking in practical metal cutting operations.

**Lack of real-time monitoring:** The study may have relied on post-cut analysis rather than real-time monitoring of chip formation and breaking. Real-time monitoring could provide more comprehensive insights into the dynamic behavior of chips and the breaking process.

It is important to recognize these limitations as they highlight areas for improvement and suggest directions for future research to make the findings more realistic and applicable to real-world metal cutting scenarios.

### **5.4 Recommendations for future research**

Recommendations for future research could include:

- Investigating the effect of different cutting tool coatings on chip formation and breaking, as well as the resulting surface finish of the workpiece.

- Studying the effect of varying cutting tool geometries, such as rake angle, on chip formation and breaking in more detail.
- Exploring the use of different lubricants or cutting fluids on chip formation and breaking, and their impact on machining performance.
- Investigating the applicability of the developed model to other materials and machining processes, to assess its wider use in industry.
- Studying the impact of machine tool vibrations on chip formation and breaking, as this can have a significant effect on surface finish and tool life.

## **5.5 Conclusion**

In conclusion, this study aimed to investigate the chip formation and breaking process in metal cutting and provide insights into the chip morphology under various cutting parameters. The experimental results revealed the significant influence of cutting speed, feed rate, and depth of cut on the chip formation and breaking process, as observed through chip morphology analysis. Additionally, the cutting tool geometry, specifically the rake angle and relief angle, played a crucial role in shaping the chip morphology.

The findings of this study have important implications for the manufacturing industry. By optimizing the machining parameters based on the observed chip morphology, manufacturers can enhance machining performance, reduce tool wear, and increase productivity. It is worth noting that the scope of this study was limited to a specific cutting tool and material, and further research is recommended to validate these findings across a wider range of cutting tools and materials.

In summary, this study contributes to our understanding of the chip formation and breaking process in metal cutting. The observed chip morphology provides valuable insights into the underlying mechanisms, which can guide the design of cutting tools and the optimization of machining parameters. These findings have the potential to drive improvements in efficiency and productivity within the manufacturing industry.

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## APPENDICES

### List of Mathematical Models and Equations

#### 1. Specific cutting force equation

The specific cutting force (K) can be calculated using the following equation:

$$K = F_c / A_e$$

Where  $F_c$  is the cutting force and  $A_e$  is the area of the undeformed chip cross-section.

#### 2. Shear angle equation

The shear angle ( $\alpha$ ) can be calculated using the following equation:

$$\tan(\alpha) = (\sin(\varphi) - \mu \cos(\varphi)) / (\cos(\varphi) + \mu \sin(\varphi))$$

Where  $\varphi$  is the rake angle and  $\mu$  is the coefficient of friction.

#### 3. Chip thickness equation

The chip thickness (t) can be calculated using the following equation:

$$t = f * a_p$$

Where f is the feed rate and  $a_p$  is the depth of cut.

#### 4. Cutting power equation

The cutting power (P) can be calculated using the following equation:

$$P = F_c * v_c$$

Where  $v_c$  is the cutting speed.

#### 5. Johnson-Cook material model

The Johnson-Cook material model can be used to determine the flow stress of the material being cut. It is represented by the following equation:

$$\sigma = [A + B(\epsilon_p)^n] [1 + C \ln(\epsilon_p)] [1 - (T - T_0) / (T_m - T_0)]^m$$

Where  $\sigma$  is the flow stress, A, B, C, n, and m are material constants,  $\epsilon_p$  is the plastic strain, T is the temperature,  $T_0$  is the reference temperature, and  $T_m$  is the melting temperature.

#### 6. Chip curl radius equation

The chip curl radius ( $R_c$ ) can be calculated using the following equation:

$$R_c = t / (2 \tan(\alpha))$$

Where t is the chip thickness and  $\alpha$  is the shear angle.

#### 7. Chip segment length equation

The chip segment length ( $l$ ) can be calculated using the following equation:

$$l = \pi R_c / \sin(\alpha)$$

Where  $R_c$  is the chip curl radius and  $\alpha$  is the shear angle.

#### 8. Chip area ratio equation

The chip area ratio ( $\eta$ ) can be calculated using the following equation:

$$\eta = A_a / A_e$$

Where  $A_a$  is the area of the deformed chip cross-section and  $A_e$  is the area of the undeformed chip cross-section.

#### 9. Chip segmentation frequency equation

The chip segmentation frequency ( $f$ ) can be calculated using the following equation:

$$f = v_c / l$$

Where  $v_c$  is the cutting speed and  $l$  is the chip segment length.

#### 10. Cutting force coefficient equation

The cutting force coefficient ( $K_c$ ) can be calculated using the following equation:

$$K_c = F_c / (a_p^m * v_c^n)$$

Where  $F_c$  is the cutting force,  $a_p$  is the depth of cut,  $v_c$  is the cutting speed, and  $m$  and  $n$  are constants.